

**Course Offered in Spring Semester Department of Mathematics**

<b>Batch 2018-20, Semester-IV</b>					
<b>S. N.</b>	<b>Course Name</b>	<b>Course Code</b>	<b>Credit</b>	<b>Lecture &amp; Tutorial</b>	<b>Name of Faculty</b>
1	Fluid Dynamics	IAM 405	04	4L, 2T	Dr R Kumar
2	Differential Geometry	IAM 407	04	4L, 2T	Dr S K Srivastava
3	Operational Research	MTH 502	04	4L, 2T	Guest Faculty
4	Functional Analysis	IAM-501	04	4L, 2T	Guest Faculty
5	M. Sc. Project	MTH 550	04	4L, 2T	Dr S K Srivastava Group A
					Dr R Kumar Group B

# **Semester IV**

**Credits Equivalent:** 04 Credits (One credit is equivalent to 10 hours of lectures / organised classroom activity / contact hours; 5 hours of laboratory work / practical / field work / Tutorial / teacher-led activity and 15 hours of other workload such as independent individual/ group work; obligatory/ optional work placement; literature survey/ library work; data collection/ field work; writing of papers/ projects/dissertation/thesis; seminars, etc.)

## **Attendance Requirements:**

Students are expected to attend all lectures in order to be able to fully benefit from the course. A minimum of 75% attendance is a must failing which a student may not be permitted to appear in examination.

## **Evaluation Criteria:**

1. Mid Term Examination: 25%
2. End Term Examination: 50%
3. Counselling, Activities and Tutorials (CAT): 25%
  - i. Subjective / Objective Assignment: 10 %
  - ii. Numerical Assignments using programming: 10 %
  - iii. Presentations and Class Tests: 5 %

**Course Name: Fluid Dynamics**

**Course Code: IAM 405**

**Credits: 04**

## **Course Contents:**

**Unit I:** Basic Concepts, Orthogonal Curvilinear Coordinates, Kinematics of Fluid in Motion, General Theory of Stress and Strain, Equations of Motion of Inviscid Fluids, Bernoulli's Equation and its Applications.

**Unit II:** The Navier-Stokes Equations and the Energy Equation, Dynamical Similarity, Inspection Analysis and Dynamical Analysis:- Rayleigh's Technique and Buckingham  $\pi$ -Theorem.

**Unit III:** Laminar Flow of Viscous Incompressible Fluids with Temperature Distribution:-Plane Couette Flows, Plane Poiseuille Flows, Generalized Plane Couette Flows, Hagen-Poiseuille Flow, Flow in Tubes of Various Cross-Sections, Jeffery-Hamel Flow, Flow of two Immiscible Fluids, Flow with Constant Fluid Properties and with Variable Viscosity, and Flow in the Neighbourhood of a Stagnation Point.

**Unit IV:** Boundary Layer Theory: Velocity and Thermal Boundary Layers.

**Prescribed Text Books:**

1. Bansal J. L. (2004). Viscous Fluid Dynamics. Second Edition. Oxford and IBH Publishing, Delhi.
2. Raisinghania M.D. (2011). Fluid Dynamics. Tenth Edition. S Chand & Company LTD. New Delhi.

**Suggested Additional Readings:**

1. Schlichting H. and Gersten K. (2000). Boundary Layer Theory. Eighth Edition. Springer Verlag, Germany.
2. Kundu P.K. and Cohen I.M. (2010). Fluid Mechanics. Fourth Edition. Academic Press.

**Course Name:** Differential geometry

**Course Code:** IAM 407

**Credits:** 04

**Course Contents:**

**Unit I:** Curve, Arc-length, Reparametrization, Level curves, Curvature of Plane curve, Frenet-Formulas.

**Unit II:** Global Properties of Curves: Simple closed curves, The Isoperimetric Inequality, Four vertex Theorem, Surfaces in Euclidean Spaces, Length of curves on surface, Isometries and conformal mappings of surfaces, Surface area.

**Unit III:** The Second Fundamental Form, Curvature of curves on surface, Normal and Principal Curvatures, Gaussian and Mean curvatures.

**Unit IV:** The Pseudosphere, Gauss map, Geodesics: Basic Properties, Theorema Egregium and Gauss-Bonnet Theorem.

**Prescribed Text Books:**

Andrew Pressley, Elementary Differential Geometry, Springer, 2010.

**Suggested Additional Readings:**

M.P. doCarmo, Differential Geometry of Curves and Surfaces, Prentice Hall, 1976.

B. O'Neill, Elementary Differential Geometry, Academic Press, New York, 1966.

**Course Name: OPERATIONAL RESEARCH**

**Course Code: MTH 502**

**Credits: 04**

## **Course Contents:**

### **Unit I:**

Linear programming problem (LPP). Formulation and examples, feasible, basic feasible and optimal solutions. Graphical method to solve LPP. Simplex method, Charnes Big M method, two phase method, degeneracy. Duality theory, dual LPP, fundamental properties of dual problems, dual simplex algorithm.

### **Unit II:**

**Integer programming:** gomory's method, branch and bound method.

**Transportation problem:** Mathematical formulation, basic feasible solution of T.P. by North West corner method, least cost method, Vogle's approximation method. Unbalanced TP UV method, degeneracy in TP.

### **Unit III:**

**Assignment Problem:** Mathematical formulation, assignment method, Hungarian method, unbalanced AP.

**Network techniques:** Shortest path model, dijkstra algorithm, spanning trees, minimum spanning trees, Kruskal's algorithm, Prim's algorithm.

### **Unit IV:**

**Game theory:** Two person zero sum games, the maxmin-minmax principle, pure strategies, mix strategies, graphical solution of 2xn and mx2 games, dominance property, general solution of mxn rectangular games, LPP of GP

### **Prescribed Text Book:**

1. S.D. Sharma, operations research, kedar nath ram Nath and co. 14<sup>th</sup> edition 2004.
2. Kanti swarup, PK Gupta and Manmohan operations research, sultan chand and sons 12<sup>th</sup> edition, 2004.
3. R. paneerselvam , operations research, prentice hall of india pvt ltd, 2004.

### **Suggested Additional Readings:**

1. G. Hadley, linear programming , Narosa pub. House, 2002.
2. H.A. Taha operations research , An introduction prentice hall of india pvt ltd, 7<sup>th</sup> edition 2004.
1. J.K. sharma, operations research, macmillan India pvt ltd 2003

**Course Name: Functional Analysis**

**Course Code: IAM-501**

**Credits: 04**

**Course Contents:**

**Unit I**

Banach Spaces: The definition and some examples, continuous linear transformations. The Hahn- Banach Theorem (statement only), the Open Mapping Theorem, the Closed Graph Theorem.

**Unit II**

The Uniform Boundedness Theorem, The natural embedding of  $N$  in  $N^{**}$ , reflexivity. Hilbert Spaces: The definition and some simple properties, orthogonal complements, orthonormal sets.

**Unit III**

The conjugate space  $H^*$ , the adjoint of an operator, self-adjoint, normal and unitary operators, Projections.

**Unit IV**

Spectral Theory: Spectral Theory in Finite Dimensional Normed Spaces. Basic Concepts. Spectral Properties of Bounded Linear Operators. Further Properties of Resolvent and Spectrum.

**Text Books**

1. G.F. Simmons, Introduction to Topology and Modern Analysis, International Student Edition, McGraw Hill Book Company, Inc. 1963, (Chapter 9: §§ 46-51 and Chapter 10: §§ 52-59).
2. E. Kreyszig, Introductory Functional Analysis with Applications, John, Wiley and Sons, Wiley Classics Library Edition Published, 1989 (Chapter 7).